In vivo validation of mathematically derived fractional flow reserve for assessing haemodynamics of coronary tandem lesions

Jihoon Kweon¹, PhD; Young-Hak Kim^{1*}, MD; Dong Hyun Yang², MD; June-Goo Lee², PhD; Jae-Hyung Roh¹, MD; Gary S. Mintz³, MD; Seung-Whan Lee¹, MD; Seong-Wook Park¹, MD

1. Department of Cardiology, University of Ulsan College of Medicine, Asan Medical Center, Seoul, South Korea; 2. Department of Radiology, University of Ulsan College of Medicine, Asan Medical Center, Seoul, South Korea; 3. Cardiovascular Research Foundation, New York, NY, USA

KEYWORDS

- coronary artery
- flow bifurcation • fractional flow
- reserve
- •prediction model
- tandem lesion

Abstract

Aims: Our aim was to propose a prediction model for the post-stenting fractional flow reserve (FFR $'_{\text{dnred}}$) at a position distal to the tandem lesion.

Methods and results: Using the FFR at a position proximal to the tandem lesion (FFR_p), and the FFR gradients across proximal ($\triangle FFR$ _p) and distal ($\triangle FFR$ _d) stenoses, FFR'_{d,pred} after treating either the distal or proximal lesion was predicted as $FFR_p - \Delta FFR_p/(1-1.33k\Delta FFR_d)$ or $FFR_p - \Delta FFR_d/(1-1.33\Delta FFR_p)$, respectively. The flow fraction of the distal main branch (k) was estimated using the diameter ratio of side to distal main branches. For *in vivo* validation, 50 patients with a tandem lesion (diameter stenosis >50%) were evaluated. Compared to the conventional model that did not consider side branch flow, our predicted FFR showed closer correlation with the measured FFR ($R^2=0.83$ vs. 0.57) and significant reduction in mean absolute errors $(0.034\pm0.028 \text{ vs. } 0.053\pm0.049, \text{ p} < 0.001)$. In particular, with a large side branch and low baseline FFR, decision making using the current model had greater predictive ability than with the conventional model.

Conclusions: By predicting which stenosis is more severe and/or whether the remaining lesion after the first treatment is functionally significant, a tandem prediction model can help to plan optimised stent implantation.

**Corresponding author: Asan Medical Center, 88, Olympic-ro 43-Gil, Songpa-gu, Seoul, 138-736, South Korea. E-mail: mdyhkim@amc.seoul.kr*

Abbreviations

Introduction

Although lesion-specific fractional flow reserve (FFR) is a reliable index for assessing the haemodynamic significance of coronary artery stenosis¹, a simple FFR measurement cannot predict the true functional severity of each individual stenosis in a tandem lesion (defined as serial stenoses within one coronary artery) due to mutual flow interaction between the stenoses2 . In terms of optimal treatment sequence, previous studies have recommended that treatment of the stenosis with greater pressure or FFR gradient during pressure wire pullback should be prioritised. Therefore, because the functional severity of the remaining lesion can only be accurately assessed after treatment, a repeated FFR measurement is essential for further decision making^{3,4}.

Editorial, see page 1322

Previous studies using flow phantoms, animal models, and human patients⁵⁻⁷ have proposed theoretical equations for predicting the post-stenting FFR. However, these approaches were based on the assumption that there is no side branch between stenoses and that therefore there is a uniform flow rate across stenoses. Considering that the presence of a side branch significantly affects flow recovery after revascularisation and influences the distal pressure increase^{6,8}, an approach that more accurately reflects coronary haemodynamic conditions is necessary. By predicting how many stents are needed and/or which stenosis is more severe, such an approach can help in the planning of optimised stent implantation and facilitate the stent procedure.

The aims of our present study were: 1) to develop and validate a mathematical model of tandem lesions to predict post-stenting FFR across the remaining stenosis, and 2) to propose a relevant approach for optimal treatment.

Methods

DEFINITION

FFR is defined as the ratio of mean coronary pressure to mean aortic pressure at maximal hyperaemia. The FFR gradient across an individual stenosis is represented as Δ FFR (Δ FFR_p=FFR_p-FFR_m and $\Delta FFR_d = FFR_m - FFR_d$) (Figure 1). The primary target lesion was defined as the lesion with a larger ΔFFR between the proximal and distal stenoses. FFR (pre-procedure) and FFR′ (post-treatment of the primary target lesion) were obtained from initial and repeated pullback measurements, respectively.

DEVELOPMENT OF THE TANDEM PREDICTION MODEL

Figure 1A shows serial stenoses with an interposed side branch. Because the pressure gradient across normal lesions is negligible⁹, the distal pressures of the main and side branches are P_d and P_m , respectively. At maximum vasodilation, the flow rate to each branch is proportional to the difference between the distal pressure

Figure 1. *Changes in haemodynamic parameters after stenting. A) Before treatment. B) After distal treatment. C) After proximal treatment. D) After both treatments. Coronary flow rate (Q) is denoted by subscripts according to location (0, ostium; 1, main branch; 2, side branch) and lesion (d: distal; p: proximal; t: tandem). ′: after stenting a stenosis; ′′: after stenting both stenoses; FFR: fractional flow reserve; FFR^p ,* $FFR_{m'}$ and $FFR_{d'}$ FFR values defined at the locations corresponding to P_p , P_m , and P_d , respectively; P_a : mean aortic pressure; P_p , P_m , and P_d : *mean coronary pressures at positions proximal to the tandem lesion, between stenoses, and distal to the tandem lesion, respectively*

and the wedge pressure (P_w) . By introducing resistances R_1 and R_2 , the flow rates to the main and side branches are defined as

$$
Q_{t1} = (P_d - P_w)/R_1
$$
 and $Q_{t2} = (P_m - P_w)/R_2$,

respectively. P_w is assumed to be the same for the main and side branches. After stenting the distal stenosis **(Figure 1B)**, the distal pressure is changed to P'_m . The flow rates to the main and side branches become

$$
Q_{pl}=(P_m'-P_w')/R_1
$$
 and $Q_{p2}=(P_m'-P_w')/R_2$

,

.

respectively, where P'_{w} is the wedge pressure post stenting. Likewise, after treating the proximal stenosis **(Figure 1C)**, the distal pressure is changed to P'_{d} . Correspondingly, the flow rate to the main branch becomes

$$
Q_{dl} = (P'_d - P'_w)/R_1.
$$

To predict the FFR gradient across the proximal stenosis after stenting the distal stenosis, the linear relationship between the flow rate and the trans-stenotic pressure gradient is assumed as

$$
\frac{P_a - P_m}{P'_a - P'_m} = \frac{Q_{t1} + Q_{t2}}{Q_{p1} + Q_{p2}} = \frac{(P_d - P_w) / R_1 + (P_m - P_w) / R_2}{(P'_m - P'_w) / R_1 + (P'_m - P'_w) / R_2}.
$$

By dividing with P_{a}/P'_{a} and using the substitutions

$$
P_{d}/P_{a} \! = \! 1\! - \! \Delta \mathrm{FFR}_{p} \! - \! \Delta \mathrm{FFR}_{d} , \, P_{m}/P_{a} \! = \! 1\! - \! \Delta \mathrm{FFR}_{p} \, \, \text{and} \, \, P_{m}^{\prime}/P_{a}^{\prime} \! = \! 1\! - \! \Delta \mathrm{FFR}_{p}^{\prime},
$$

(E1)
$$
\frac{\Delta \text{FFR}_p}{\Delta \text{FFR}_p'} = \frac{(1 - \Delta \text{FFR}_p - \Delta \text{FFR}_d) / R_1 + (1 - \Delta \text{FFR}_p) / R_2 - P_w / P_a R_1 - P_w / P_a R_2}{(1 - \Delta \text{FFR}_p') / R_1 + (1 - \Delta \text{FFR}_p') / R_2 - P_w' / P_a' R_1 - P_w' / P_a' R_2}.
$$

For simplicity, we define two coefficients as

(E2) $C_1 = (1/R_1 + 1/R_2)(1-P_w/P_a) = (1/R_1 + 1/R_2)(1-P_w/P_a)$ and $C_2 = 1/R_1 + 1/R_2$.

For C_1 , the relationship between the aortic and wedge pressures is approximated as $(P_w - P_v)/(P_a - P_v) \approx P_w/P_a = constant$, where P_v is the central venous pressure⁹. Using C_1 and C_2 , equation (E1) is expressed as

$$
\frac{\Delta \text{FFR}_p}{\Delta \text{FFR}_p'} = \frac{C_1 - C_2 \Delta \text{FFR}_p - \Delta \text{FFR}_d / R_1}{C_1 - C_2 \Delta \text{FFR}_p'}
$$

By multiplying $(C_1 - C_2 \Delta FFR_p')/\Delta FFR_p$,

$$
\frac{C_1}{\Delta FFR_p'} - C_2 = \frac{C_1 - \Delta FFR_a / R_1}{\Delta FFR_p} - C_2.
$$

By cancelling C_2 and taking the inverse,

(E3)
$$
\Delta FFR'_{p} = \frac{\Delta FFR_{p}}{1 - \Delta FFR_{d}/R_{1}C_{1}}.
$$

For the prediction of Δ FFR'_d, the linear relationship between the flow rate and the pressure gradient across the distal stenosis yields

$$
\frac{P_{m}-P_{d}}{P_{a}^{'}-P_{d}^{'}}=\frac{Q_{t1}}{Q_{d1}}\!=\!\frac{\left(P_{d}-P_{w}\right)/\,R_{1}}{\left(P_{d}^{'}-P_{w}^{'}\right)/\,R_{1}}
$$

.

,

By dividing with P_{a}/P'_{a} and using the substitutions $P_d/P_a = 1 - \Delta FFR_p - \Delta FFR_d$ and $P'_d/P'_a = 1 - \Delta FFR'_d$

$$
\frac{\Delta \text{FFR}_{d}}{\Delta \text{FFR}'_{d}} = \frac{1 - \Delta \text{FFR}_{p} - \Delta \text{FFR}_{d} - P_{w} / P_{a}}{1 - \Delta \text{FFR}'_{d} - P'_{w} / P'_{a}}.
$$

For simplicity, we define a coefficient as

$$
C_3 = 1 - P_w / P_a = 1 - P_w / P_a'
$$

and equation (E4) becomes

$$
\frac{\Delta \text{FFR}_{d}}{\Delta \text{FFR}'_{d}} = \frac{C_{3} - \Delta \text{FFR}_{p} - \Delta \text{FFR}_{d}}{C_{3} - \Delta \text{FFR}'_{d}}.
$$

Rearrangement gives

$$
\frac{C_3}{\Delta FFR'_d} - 1 = \frac{C_3 - \Delta FFR_p}{\Delta FFR_d} - 1,
$$

and therefore

(E5)
$$
\Delta FFR_d' = \frac{\Delta FFR_d}{1 - \Delta FFR_p/C_3}.
$$

To estimate C_1 and C_2 , the coronary bifurcation after stenting both stenoses is considered **(Figure 1D)**. In ideal conditions, the distal pressure recovers to the mean aortic pressure (P''_a) . Therefore, the flow rates to the main and side branches are

 $(E6)$ $=(P''_{a}-P''_{w})/R_{1}$ and $Q_{1}=(P''_{a}-P''_{w})/R_{2}$,

respectively. P''_w is the corresponding wedge pressure. Using the equation (E6), the term $1/R_1+1/R_2$ in C₁ can be expressed as

$$
\frac{1}{R_1} + \frac{1}{R_2} = \frac{Q_1 + Q_2}{P_a'' - P_w''}
$$

By substituting $1/R_1 + 1/R_2$ into equation (E2),

$$
C_1 = \frac{Q_1 + Q_2}{P_a'' - P_w''} \big(1 - P_w \; / \; P_a \, \big) = \frac{Q_1 + Q_2}{P_a'' - P_w''} \big(1 - P_w'' \; / \; P_a'' \big) = \frac{Q_0}{P_a''}.
$$

By multiplying R_1 and taking the inverse,

$$
\frac{1}{R_1C_1} = \frac{Q_1}{P_a'' - P_w''} \frac{P_a''}{Q_0} = \frac{Q_1}{Q_0} \frac{P_a''}{P_a'' - P_w''}
$$

By defining $w=1/C_3 = P''_a/(P''_a-P''_w) = P_a/(P_a-P_w)$ and $k=Q_1/Q_0$, equations (E3) and (E5) finally become

(E7)
$$
\Delta FFR'_p = \frac{\Delta FFR_p}{1 - \text{kw} \times \Delta FFR_d}
$$
 and $\Delta FFR'_d = \frac{\Delta FFR_d}{1 - \text{w} \times \Delta FFR_p}$.

In the present study, P_w/P_a was assumed to be 0.25⁶, and correspondingly w=1.33. The uncertainty associated with P_w was assessed by evaluating the variations in Δ FFR'_p using the published standard deviation $(P_w/P_a=0.25\pm 0.10)^6$. The estimated error in FFR prediction was ≤ 0.02 for FFR_d > 0.6 .

VALIDATION OF THE TANDEM PREDICTION MODEL

For tandem lesions, the distal FFR after the treatment of the distal or proximal stenosis is predicted as

$$
FFR'_{d,pred} = FFR_p - \frac{\Delta FFR_p}{1 - 1.33k \times \Delta FFR_d} \text{ or } FFR_p - \frac{\Delta FFR_d}{1 - 1.33 \times \Delta FFR_p},
$$

respectively ("current model"). k is the flow fraction of the distal main branch at the bifurcation point. To validate our mathematical models, the distal FFR measured after treating the primary target lesion (FFR'_{d}) was compared with the predicted FFR value (FFR $^{\prime}$ _{d,pred}). The baseline FFR values were calculated from the initial pullback measurement. k was estimated with the allometric

Intervention 2016;12: e**1375-** e**1384**

Euro

scaling law of flow bifurcation¹⁰ using the diameters of coronary branches obtained by quantitative coronary angiography (QCA) **(Figure 2)**. If multiple side branches were positioned in the tandem lesion, only the largest one was considered.

To compare prediction accuracy, predicted FFR values were computed by applying the "conventional model",

$$
FFR'_{d, pred} = \frac{P_d - (P_m/P_a) \times P_w}{P_a - P_m + P_d - P_w} \ \ \text{or} \ \ 1 - \frac{(P_a - P_w) \times (P_m - P_d)}{P_a \times (P_m - P_w)} \, ,
$$

for the treatment of proximal or distal stenosis, respectively⁵. The wedge pressure was estimated using the assumption of $P_{w}/P_{a} = 0.25$, as in the current model.

Figure 2. Plot of k vs. d_1/d_1 . k: flow fraction of the distal main branch *at the bifurcation point of interest; d₂/d₁: diameter ratio of side to distal main branches at the branching point (normal segment)*

STUDY SUBJECTS FOR MODEL VALIDATION

From November 2011 to May 2015, a total of 82 patients who had coronary tandem lesions with an FFR <0.80 at a position distal to the distal stenosis were retrospectively selected from the prospective FFR registry. A tandem lesion was defined as two separate stenoses within one epicardial coronary artery, each with a stenosis diameter >50% by visual estimation and separated by an angiographically normal segment. After excluding patients with acute coronary syndrome, significant left main coronary artery disease, incomplete stent coverage of the target lesion, coronary spasms, in-stent restenosis, left ventricular ejection fraction <40%, regional wall motion abnormalities, or coronary artery bypass grafts, 50 tandem lesions from 50 patients with complete angiographic and serial FFR data sets were analysed.

CORONARY ANGIOGRAPHIC AND FFR MEASUREMENT

Catheterisation was performed through the femoral or radial route using standard catheters. Coronary angiograms were digitally recorded and quantitatively assessed in the Angiographic Core Laboratory (Asan Medical Center, Seoul, South Korea), using an automated edge detection system (CAAS II; Pie Medical, Maastricht, The Netherlands). QCA analysis was conducted by experienced personnel according to standard clinical definitions¹¹.

FFR measurements were performed using 0.014 inch pressure wires (St. Jude Medical, St. Paul, MN, USA) following standard procedures¹². Under fluoroscopic guidance, the pressure wire was advanced into the coronary artery of interest to a position distal to the most distal stenosis, and steady-state maximum hyperaemia was induced by the continuous administration of 140-200 μm/kg/min adenosine into the large antecubital vein or the central vein. During maximal hyperaemia, the pressure wire was slowly pulled back to the ostium of the coronary artery while longitudinal pressure changes were recorded. The FFR values were automatically displayed, and all pressure tracings were recorded by a RadiAnalyzer™ Xpress (St. Jude Medical) for offline analysis. Finally, the pressure wire was completely pulled back into the guiding catheter to verify that no drift had occurred during the procedure.

After FFR measurement, percutaneous coronary intervention (PCI) for functionally significant tandem lesions ($FFR_d< 0.80$) was performed. First, a drug-eluting stent was implanted at the primary target lesion with the greater ΔFFR. Then, to assess the functional severity of the remaining stenosis, FFR'_{d} was measured at the same position where FFR_d was measured pre stenting. When FFR'_d was <0.80, the remaining stenosis was treated by placing another stent. All procedures, including stent sizing and optimisation, were performed with intravascular ultrasound guidance.

STATISTICAL ANALYSIS

Continuous variables are presented as mean±SD, and categorical variables are presented as numbers and percentages. Linear regression analysis was performed to compare $\text{FFR}'_{\text{d,pred}}$ with FFR'_{d} . Bland-Altman analysis was used to calculate the bias and limits of agreement between $\text{FFR}'_{d,pred}$ - FFR'_d and FFR'_d . To compare the prediction models, a paired t-test and Wilcoxon signed-rank test were applied to the prediction error (FFR $'_{d \text{ pred}}$ –FFR'_d) and its absolute value ($|{\rm FFR'}_{d,pred} - {\rm FFR'}_{d}|$), respectively. Values of p<0.05 were considered statistically significant and normality of data was tested with the Shapiro-Wilk W-test (p>0.05). The Durbin-Watson statistic was calculated to test for a serial autocorrelation of the error terms in the regression models. All statistical analyses were performed using SPSS, Version 17.0 for Windows (SPSS, Inc., Chicago, IL, USA).

Results

PATIENTS

The baseline clinical, QCA, and FFR data in 50 patients with 50 tandem lesions are summarised in **Table 1** and **Table 2**. The proximal stenosis was treated first in 27 (54%) patients, while the distal

Table 1. Baseline clinical characteristics of 50 patients.

stenosis was treated first in the remaining 23 (46%) patients. In 37 (74%) patients, only a single stenosis was treated, with deferral of the remaining lesion.

PREDICTION ACCURACY COMPARED TO A CONVENTIONAL MODEL

The correlation between predicted and measured post-stenting FFR′ values and the accuracy of the prediction models are shown in **Figure 3**. The current prediction model (vs. conventional) showed a closer correlation with the measured FFR $(R²=0.83$ vs. 0.57). Correspondingly, our current model reduced the standard deviation of prediction errors by half $(0.029 \pm 0.033$ vs. 0.027 ± 0.068 , p=0.769) and had a greater prediction power in terms of absolute prediction errors (0.034±0.028 vs. 0.053±0.049, p<0.001). Also, in the ischaemia prediction of the remaining lesion (FFR $\frac{\gamma}{4}$ <0.80), our current model yielded improved accuracy (82% vs. 78%).

Decision making of tandem lesion treatment DECISION DISAGREEMENT USING BASELINE ΔFFR VS. PREDICTED FFR'

The impact of side branch flow on the post-stenting FFR gradient is shown in **Figure 4A**, which was analytically obtained from the current prediction model. When Δ FFR_p and Δ FFR_d appeared to be equal, the post-stenting $\text{FFR}'_{\text{d,pred}}$ for the treatment of distal stenosis (vs. proximal) was higher, and the difference between post-stenting $\text{FFR}'_{d,pred}$ increased with lower FFR_d and smaller k. Accordingly, disagreement in the decision making of the first target lesion using baseline ΔFFR and predicted post-stenting $\text{FFR}'_{d,\text{pred}}$ was observed, as shown in **Figure 4B**. When $[\Delta \text{FFR}_d -]$ Δ FFR_p] was >0, the treatment of distal stenosis was predicted to be more effective in reducing ischaemia. Conversely, when $[\Delta$ FFR_a $-\Delta$ FFR_p] was <0, the distal stenosis could be more severe

Table 2. QCA and FFR data in 50 tandem lesions.

and distal to the tandem lesion, respectively; k: flow fraction of the distal main branch at the bifurcation point of interest; QCA: quantitative coronary angiography

despite a larger ΔFFR across the proximal stenosis, as indicated by the "disagreement zone". The lower the FFR_d value and the higher the side branch flow, the larger the disagreement zone became.

CASE EXAMPLE

The practical application of the current prediction model is explained in **Figure 5**. In the case example, the FFR value at the position proximal to the tandem lesion was $\text{FFR}_{p} = 1$, and the FFR gradients across the proximal and distal stenoses were Δ FFR_p=0.23 and Δ FFR_d=0.08, respectively. After the estimation of k (=0.66) using the diameter ratio of side to distal main

Figure 3. *Plots of FFR′d,pred vs. FFR′^d after stenosis treatment in a tandem lesion (left column) and the corresponding Bland-Altman plot (right column) for conventional (A, B) and current (C, D) models. For the current model, k is calculated using the diameter ratio of the side to distal main branches (Figure 2). Each dot indicates a tandem lesion. The red-shaded region in the left column indicates an offset of ±0.03. ′: after treatment; FFR: fractional flow reserve; FFR_d: FFR at a position distal to the tandem lesion; pred: predicted*

Figure 4. *A disagreement in the decision making of the first target lesion using baseline ΔFFR and predicted post-stenting FFR′d,pred. When the baseline ΔFFR^d and ΔFFR^p are equal, the distal stenosis (vs. proximal) is predicted to be relatively more severe (higher FFR′d,pred for the treatment of distal stenosis) with a higher side branch flow (a smaller k) (A). When k is fixed as 0.5, the disagreement zone becomes larger* with a lower baseline FFR_a(B). ': after treatment; FFR: fractional flow reserve; ΔFFR: translesional FFR gradient; FFR_a: FFR at a position distal to the tandem lesion; ΔFFR_, and ΔFFR_a: FFR gradients across proximal and distal stenoses, respectively; k: flow fraction of the main *branch at the bifurcation point of interest; pred: predicted*

Figure 5. *Case example of the use of the current prediction model to assess a tandem lesion. Using the baseline FFR gradients (ΔFFR^p =0.23 and ΔFFR^d =0.08) and the estimated k (=0.66), the post-stenting FFR′d,pred was predicted to be 0.88 or 0.75 for the treatment of proximal or distal stenosis, respectively. After treating the proximal stenosis, the measured post-stenting FFR′^d was 0.85. FFR at a position proximal to the tandem lesion. FFR: fractional flow reserve; FFR′d: FFR distal to the tandem lesion after treatment; ΔFFR^p and ΔFFRd: FFR gradients across proximal and distal stenoses, respectively; k: flow fraction of the distal main branch at the bifurcation point of interest; pred: predicted; QCA: quantitative coronary angiography*

branches ($d_2/d_1 = 0.80$), the FFR'_{d,pred} was predicted to be 0.88 or 0.75 for the treatment of proximal or distal stenosis, respectively. The predicted $FFR'_{d,med}$ indicated that the treatment of proximal stenosis was more effective and the treatment of distal stenosis was not necessary. For this patient, only the proximal stenosis was treated, and the measured post-stenting FFR'_{d} was 0.85.

UTILISATION OF A ΔFFR MAP

To facilitate clinical decision making, optimal treatment strategies for tandem lesions were suggested by the ∆FFR map based on the current prediction model in which the baseline distal FFR was functionally significant (FFR_d<0.80) (Figure 6). The ΔFFR map was divided into three sub-regions by a red line (the same $\text{FFR}'_{d \text{pred}}$ for the treatment of proximal and distal stenoses), blue line (FFR $^{\prime}_{\text{d} \text{pred}}$ =0.8 for the treatment of distal stenosis) and green line (FFR $_{d,pred}^{\prime}$ =0.8 for the treatment of proximal stenosis). Accordingly, tandem lesions were categorised into "treat only distal", "treat only proximal" and "treat both". Depending on the side branch flow, the boundaries of "treat only distal" (red and blue lines) were modified, while the green line remained constant. Therefore, evaluation and comparison of FFR'_{d,pred} using the current prediction model were required in the blue area to determine whether only the distal lesion or both lesions should be treated, as well as in the orange area to decide whether the

Figure 6. *ΔFFR map for clinical decision making in tandem lesions. The evaluation and comparison of post-stenting FFR′d,pred using the current prediction model are required in the blue and orange areas, where the boundaries are dependent on k; otherwise, the decision can be directly made. Here, FFR*_p=1 is assumed, and, for the patients with FFR_p=1, the prediction accuracy of this map was 91% (20/22). *′: after treatment; FFR: fractional flow reserve; ΔFFR: translesional FFR gradient; ΔFFR_p</sub> and ΔFFR_a: FFR gradients across proximal and distal stenoses, respectively; k: flow fraction of the distal main branch at the bifurcation point of interest*

distal or proximal lesion should be treated. For the patient shown in **Figure 5**, the baseline FFR gradients (Δ FFR_p=0.23 and Δ FFR_d=0.09) indicated that only the proximal lesion should be treated.

Discussion

While FFR is reliable for assessing the haemodynamic significance of coronary artery stenosis, the functional severity of individual stenoses cannot be assessed without repeated FFR measurements in tandem lesions with an interposed side branch. Therefore, the aim of our present study was to provide and validate a mathematical prediction model for post-stenting $\text{FFR}'_{\text{d,pred}}$. The major findings of our present study were: 1) a mathematical prediction model reflecting the actual severity of individual stenoses and the effect of interposed side branches allowed us to predict post-stenting FFR′ accurately across the remaining stenosis $(R²=0.83$ between predicted vs. measured FFR'); and 2) this prediction model was helpful in deciding which stenosis was more severe and whether the remaining lesion after the first treatment was functionally significant.

Our current results showed an improvement in accuracy using the current prediction model. This may be explained by three factors. First, the effect of interposed side branches was considered in the current model. Although the conventional model achieved high prediction accuracy for tandem lesions with negligible side branches⁶, larger discrepancies were observed in the population with various sizes of side branch. Second, the conventional prediction model overestimated the ΔFFR _p by ignoring the pressure drop from the coronary ostium to the tandem lesion (FFR_p \neq 1). In 27 tandem lesions, including 22 left anterior descending arteries, consideration of FFR_{p} (0.947 \pm 0.032) improved the accuracy of our prediction model, although further evaluation of dynamic changes in FFR'_p post stenting is needed to clarify this issue7 . Third, the FFR-based (not pressure-based) calculation in our prediction model was amenable to variations in aortic pressure during the pullback measurement, independently of blood pressure¹³.

The measurement of wedge pressure (P_w) is considered a main obstacle to the clinical use of prediction models^{6,12}, and, in tandem lesions, direct measurements for both side and distal main branches are virtually impossible. In our current model, the need for wedge pressure information was eliminated with the assumption of $P_w/P_a = 0.25$. The prediction error of using the fixed P_w/P_a was demonstrated to be within the clinically acceptable range (0.02 when FFR_d >0.6). The flow bifurcation ratio (k) was also estimated without direct measurements. The plot of k vs. d_2/d_1 shown in **Figure 2** can be simply used for the estimation of k, and, for tandem lesions with no side branch, post-stenting FFR prediction can be achieved by applying k=1. Considering the prediction error associated with k estimation $(\leq 0.01$ per 0.1 of k when $FFR_d > 0.6$ in **Figure 4A**), the k value obtained with a rough estimation of the diameter ratio did not hamper the prediction accuracy, and therefore the real-time application of the

current model would be feasible in a clinical context. Moreover, the ΔFFR map that was provided based on the current prediction model facilitates immediate decision making for the optimal treatment strategy for tandem lesions. Consequently, the current model is more customised to the clinical context, allowing us to predict post-stenting FFR′ accurately without wedge pressure measurements.

A recent study reported that the FFR gradient (ΔFFR) was theoretically the same as the pressure gradient across a stenosis, but was a more feasible and practical index for comparing the relative functional severity between two separate lesions³. Thus, it has been recommended that the stenosis with the larger ΔFFR should be treated first, and that the post-stenting FFR'_{d} across the remaining stenosis should then be evaluated. However, our prediction model showed that there was a disagreement zone in which the decision making for more effective treatment was different between the evaluation of the baseline Δ FFR and the predicted post-stenting FFR'_{d,pred}. With the flow-dependent property of pressure gradients, proximal and distal stenoses mutually affect each ΔFFR. If there is no side branch between two separate lesions, the baseline ΔFFR values equally underestimate the true severities of both stenoses, and thus reveal which stenosis is more severe. However, because an increase in side branch flow attenuates the recovery of the coronary flow across the proximal stenosis after the treatment of the distal stenosis and not vice versa, equal baseline ΔFFR values imply that the distal stenosis is more severe. In the same context, the interpretation of our current model is consistent with the recent reports that stenting a downstream stenosis produced little change in the FFR gradient across the intermediate left main disease^{14,15}, because the treatment of a stenosis in the left anterior descending or left circumflex restores a fraction of the flow rate running through the left main. Nonetheless, for the FFR prediction of tandem lesions with left main diseases, further investigations should be made. These findings suggest that treatment of the proximal stenosis with a larger ΔFFR could be less effective, particularly with more severe lesions and higher side branch flow.

Furthermore, our current prediction model, unlike the simple comparison of baseline ΔFFR values, makes it possible to simulate the residual FFR after the first treatment and thus to plan for a tailored stent before the procedure. For instance, there may be technical difficulties in delivering the second stent to the distal site through the primarily stented proximal segment. If the presence of residual ischaemia is predicted and both stenoses should be treated, operators can avoid unnecessarily complex procedures by first treating the distal lesion.

Limitations

Our current study had some potential limitations. First, the small sample size and potential selection bias may have affected the results. Second, the linear relationship between the cycleaveraged pressure and flow rate could ignore the transient characteristics of coronary flows, and did not include the quadratic term associated with flow separation and turbulence around the stenosis, which may have caused an additional pressure drop^{16,17}. Third, the wedge pressures for the distal main and side branches were assumed to be equal. Fourth, our current model did not include the assessment of left main lesions with downstream stenoses and cannot be applied to lesions with more than two stenoses, multiple large side branches, or diffuse lesions. Fifth, the outcome of FFR prediction could be impaired when distal embolisation occurs as a consequence of extensive vessel manipulation or degree of platelet inhibition. Sixth, the bifurcation angle was not considered in the calculation, which could be an important determinant for the flow fraction to branches¹⁸. Finally, despite our efforts to apply the prediction model simply in daily practice, its clinical relevancy needs to be further validated with subsequent clinical studies.

Conclusion

Post-stenting FFR in tandem lesions with an interposed side branch can be accurately predicted without the measurement of wedge pressure. By predicting which stenosis is more severe and/or whether the remaining lesion after the first treatment is functionally significant, this tandem prediction model can help in planning optimised stent implantation and facilitate the stent procedure.

Impact on daily practice

Post-stenting FFR in tandem lesions with an interposed side branch can be accurately predicted without the measurement of wedge pressure. By predicting which stenosis is more severe and/or whether the remaining lesion after the first treatment is functionally significant, a tandem prediction model can help to plan optimised stent implantation.

Funding

This study was supported by a grant from the Korea Healthcare Technology R&D Project, Ministry for Health & Welfare Affairs, Republic of Korea (HI14C0517 and HI12C0630), a National Research Foundation of Korea (NRF) grant funded by the Korean government (MSIP) (NRF-2015R1A2A2A04003034), and by the Basic Science Research Program through the National Research Foundation of Korea (NRF), funded by the Ministry of Science, ICT & Future Planning (NRF-2013R1A1A1058711).

Conflict of interest statement

The authors have no conflicts of interest to declare.

References

1. Pijls NH, de Bruyne B, Peels K, van der Voort PH, Bonnier HJ, Bartunek J, Koolen JJ. Measurement of fractional flow reserve to assess the functional severity of coronary-artery stenoses. *N Engl J Med.* 1996;334:1703-8.

2. Pijls NH. Fractional flow reserve to guide coronary revascularization. *Circ J.* 2013;77:561-9.

3. Park SJ, Ahn JM, Pijls NH, De Bruyne B, Shim EB, Kim YT, Kang SJ, Song H, Lee JY, Kim WJ, Park DW, Lee SW, Kim YH, Lee CW, Park SW. Validation of functional state of coronary tandem lesions using computational flow dynamics. *Am J Cardiol.* 2012;110:1578-84.

4. Kim HL, Koo BK, Nam CW, Doh JH, Kim JH, Yang HM, Park KW, Lee HY, Kang HJ, Cho YS, Youn TJ, Kim SH, Chae IH, Choi DJ, Kim HS, Oh BH, Park YB. Clinical and physiological outcomes of fractional flow reserve-guided percutaneous coronary intervention in patients with serial stenoses within one coronary artery. *JACC Cardiovasc Interv.* 2012;5:1013-8.

5. De Bruyne B, Pijls NH, Heyndrickx GR, Hodeige D, Kirkeeide R, Gould KL. Pressure-derived fractional flow reserve to assess serial epicardial stenoses theoretical basis and animal validation. *Circulation.* 2000;101:1840-7.

6. Pijls NH, De Bruyne B, Bech GJ, Liistro F, Heyndrickx GR, Bonnier HJ, Koolen JJ. Coronary pressure measurement to assess the hemodynamic significance of serial stenoses within one coronary artery: validation in humans. *Circulation.* 2000;102:2371-7.

7. Saito N, Matsuo H, Kawase Y, Watanabe S, Bao B, Yamamoto E, Watanabe H, Nakatsuma K, Ueno K, Kimura T. In vitro assessment of mathematically-derived fractional flow reserve in coronary lesions with more than two sequential stenoses. *J Invasive Cardiol.* 2013;25:642-9.

8. Li Y, Gutiérrez-Chico JL, Holm NR, Yang W, Hebsgaard L, Christiansen EH, Mæng M, Lassen JF, Yan F, Reiber JH, Tu S. Impact of Side Branch Modeling on Computation of Endothelial Shear Stress in Coronary Artery Disease: Coronary Tree Reconstruction by Fusion of 3D Angiography and OCT. *J Am Coll Cardiol.* 2015;66:125-35.

9. Pijls N, Van Son J, Kirkeeide R, De Bruyne B, Gould K. Experimental basis of determining maximum coronary, myocardial, and collateral blood flow by pressure measurements for assessing functional stenosis severity before and after percutaneous transluminal coronary angioplasty. *Circulation.* 1993;87: 1354-67.

10. Murray CD. The physiological principle of minimum work applied to the angle of branching of arteries. *J Gen Physiol.* 1926;9: 835-41.

11. Popma JJ, Leon MB, Moses JW, Holmes DR, Cox N, Fitzpatrick M, Douglas J, Lambert C, Mooney M, Yakubov S, Kuntz RE; SIRIUS Investigators. Quantitative assessment of angiographic restenosis after sirolimus-eluting stent implantation in native coronary arteries. *Circulation.* 2004;110:3773-80.

12. Kern MJ, Lerman A, Bech JW, De Bruyne B, Eeckhout E, Fearon WF, Higano ST, Lim MJ, Meuwissen M, Piek JJ, Pijls NH, Siebes M, Spaan JA; American Heart Association Committee on Diagnostic and Interventional Cardiac Catheterization, Council on Clinical Cardiology. Physiological assessment of coronary artery disease in the cardiac catheterization laboratory: a scientific statement from the American Heart Association Committee on

Diagnostic and Interventional Cardiac Catheterization, Council on Clinical Cardiology. *Circulation.* 2006;114:1321-41.

13. Pijls NH, Van Gelder B, Van der Voort P, Peels K, Bracke FA, Bonnier HJ, El Gamal MI. Fractional flow reserve. A useful index to evaluate the influence of an epicardial coronary stenosis on myocardial blood flow. *Circulation.* 1995;92:3183-93.

14. Daniels DV, van't Veer M, Pijls NH, van der Horst A, Yong AS, De Bruyne B, Fearon WF. The impact of downstream coronary stenoses on fractional flow reserve assessment of intermediate left main disease. *JACC Cardiovasc Interv.* 2012;5: 1021-5.

15. Fearon WF, Yong AS, Lenders G, Toth GG, Dao C, Daniels DV, Pijls NH, De Bruyne B. The impact of downstream coronary stenosis on fractional flow reserve assessment of intermediate left main coronary artery disease: human validation. *JACC Cardiovasc Interv.* 2015;8:398-403.

16. Gould KL. Pressure-flow characteristics of coronary stenoses in unsedated dogs at rest and during coronary vasodilation. *Circ Res.* 1978;43:242-53.

17. Siebes M, Verhoeff BJ, Meuwissen M, de Winter RJ, Spaan JA, Piek JJ. Single-wire pressure and flow velocity measurement to quantify coronary stenosis hemodynamics and effects of percutaneous interventions. *Circulation.* 2004;109:756-62.

18. Huo Y, Finet G, Lefevre T, Louvard Y, Moussa I, Kassab GS. Which diameter and angle rule provides optimal flow patterns in a coronary bifurcation? *J Biomech.* 2012;45:1273-9.